

**GCE Subject Level
Conditions and
Requirements for Statistics**

May 2016

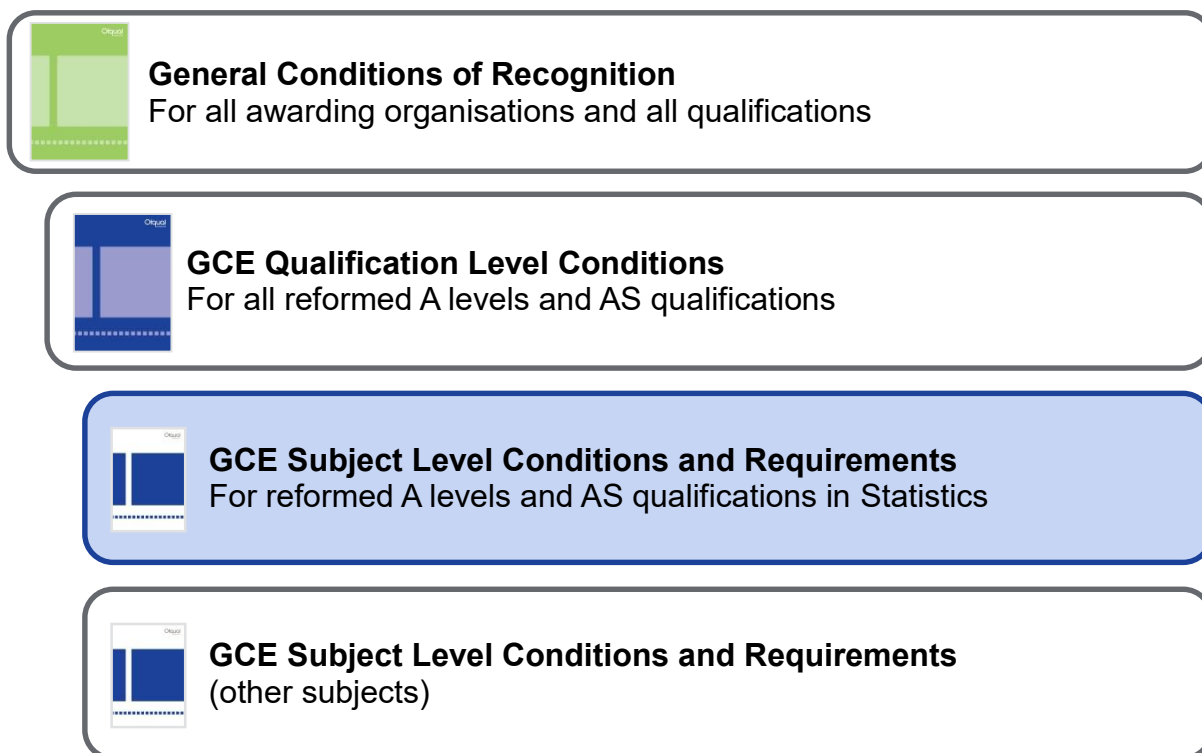
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Introduction

About this document

This document (highlighted in the figure below) is part of a suite of documents which sets out the regulatory requirements for awarding organisations offering reformed A levels and AS qualifications.



We have developed all our requirements for GCE qualifications with the intention that AS and A level qualifications should fulfil the purposes set out in the table below:

A levels	AS qualifications
<ul style="list-style-type: none"> ■ define and assess achievement of the knowledge, skills and understanding which will be needed by students planning to progress to undergraduate study at a UK higher education establishment, particularly (although not only) in the same subject area; ■ set out a robust and internationally comparable post-16 academic course of study to develop that knowledge, skills and understanding; 	<ul style="list-style-type: none"> ■ provide evidence of students' achievements in a robust and internationally comparable post-16 course of study that is a sub-set of A level content; ■ enable students to broaden the range of subjects they study.

<ul style="list-style-type: none">■ permit UK universities to accurately identify the level of attainment of students;■ provide a basis for school and college accountability measures at age 18; and■ provide a benchmark of academic ability for employers.	
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Requirements set out in this document

This document sets out the GCE Subject Level Conditions for Statistics. These conditions will come into effect at 5.01pm on Tuesday 17 May 2016 for the following qualifications:

- all GCE A levels in Statistics awarded on or after 1 April 2019; and
- all standalone GCE AS qualifications in Statistics awarded on or after 1 April 2018.

It also sets out our requirements in relation to assessment objectives – awarding organisations must comply with these requirements under Condition GCE(Statistics)1.2.

Appendix 1 reproduces the subject content requirements for Statistics, as published by the Department for Education.¹ Awarding organisations must comply with these requirements under Condition GCE(Statistics)1.1.

With respect to the qualifications listed above, awarding organisations must also comply with:

- our *General Conditions of Recognition*,² which apply to all awarding organisations and qualifications;
- our *GCE Qualification Level Conditions and Requirements*,³ and

¹ www.gov.uk/government/publications/gce-as-and-a-level-statistics

² www.gov.uk/government/publications/general-conditions-of-recognition

³ www.gov.uk/government/publications/gce-qualification-level-conditions-and-requirements

- all relevant Regulatory Documents.⁴

With respect to all other GCE qualifications in Statistics, awarding organisations must continue to comply with the General Conditions of Recognition, the *GCE Qualification Level Conditions*,⁵ and the relevant Regulatory Documents.

Summary of requirements

Subject Level Conditions	
GCE(Statistics)1	Compliance with content requirements

Assessment objectives
Assessment objectives – GCE Qualifications in Statistics

Appendix 1 – Subject content (published by Department for Education)
GCE AS and A level Subject Content for Statistics

⁴ www.gov.uk/guidance/regulatory-document-list

⁵ www.gov.uk/government/publications/gce-qualification-level-conditions-for-pre-reform-qualifications

Subject Level Conditions

GCE Subject Level Conditions for Statistics

Condition

Compliance with content requirements

GCE(Statistics)1

GCE(Statistics)1.1

In respect of each GCE Qualification in Statistics which it makes available, or proposes to make available, an awarding organisation must –

- (a) comply with the requirements relating to that qualification set out in the document published by the Secretary of State entitled ‘Statistics GCE AS and A level subject content’,⁶ document reference DFE-00059-2016,
- (b) have regard to any recommendations or guidelines relating to that qualification set out in that document, and
- (c) interpret that document in accordance with any requirements, and having regard to any guidance, which may be published by Ofqual and revised from time to time.

GCE(Statistics)1.2

In respect of each GCE Qualification in Statistics which it makes available, or proposes to make available, an awarding organisation must comply with any requirements, and have regard to any guidance, relating to the objectives to be met by any assessment for that qualification which may be published by Ofqual and revised from time to time.

⁶ www.gov.uk/government/publications/gce-as-and-a-level-statistics

Assessment objectives

Assessment objectives – GCE Qualifications in Statistics

Condition GCE(Statistics)1.2 allows us to specify requirements relating to the objectives to be met by any assessment for GCE Qualifications in Statistics.

The assessment objectives set out below constitute requirements for the purposes of Condition GCE(Statistics)1.2. Awarding organisations must comply with these requirements in relation to all GCE Qualifications in Statistics they make available.

	Objective	Weighting (A level)	Weighting (AS)
AO1	Demonstrate knowledge and understanding, using appropriate terminology and notation, of standard statistical techniques used – <ul style="list-style-type: none"> ■ to collect and represent data ■ to calculate summary statistics and probabilities ■ in relation to hypotheses and inference. 	55%	55%
AO2	Interpret statistical information and results in context and reason statistically to make predictions, construct arguments, make decisions and draw conclusions.	25%	25%
AO3	Critically assess the reliability and validity of statistical methodologies and the conclusions drawn through the application of the statistical enquiry cycle.	20%	20%

In designing and setting each set of assessments⁷ for a GCE Qualification in Statistics which it makes available, or proposes to make available, an awarding organisation must –

⁷ For the purposes of this requirement a 'set of assessments' means the assessments to be taken by a particular Learner for a GCE Qualification in Statistics. For clarity, the assessments taken by Learners may vary, depending on any possible routes through the qualification.

- take reasonable steps to achieve the weighting specified above for each of the assessment objectives, and
- where it is not possible to achieve those weightings having taken reasonable steps, ensure that the weighting of each of assessment objectives AO1 to AO3 is within +/- 2% of the relevant weighting specified above.

Subject content (published by Department for Education)



Department
for Education

Statistics

GCE AS and A level content

March 2016

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The content for AS and A level statistics

Introduction

1. The AS and A level subject content sets out the knowledge, understanding and skills common to all specifications in AS and A level statistics. Together with the assessment objectives it provides the framework within which awarding organisations create the detail of the specifications.

Aims and objectives

2. A level statistics builds upon the statistics and probability components of GCSE mathematics and employs the statistical enquiry cycle to help make sense of data trends and to solve statistical problems in a variety of contexts, such as psychology, biology, geography, business and the social sciences. It prepares students for further study and employment in a wide range of disciplines which use statistical analysis and reasoning with data. The AS statistics is a subset of the A level, which is aimed specifically at facilitating the development of the statistical elements employed across the A level curriculum and supports transition to higher education or employment in any of the many disciplines that make use of quantitative analysis.

3. AS and A level specifications in statistics must encourage students to:

- understand the application of techniques within the framework of the statistical enquiry cycle and the research methodologies used in experiments and surveys
- apply statistical techniques to data sourced from a variety of contexts, appreciating when samples or population data could be used and applying appropriate sampling techniques
- generate and interpret the diagrams, graphs and measurement techniques used in performing statistical investigations
- have an understanding of how visualisations of multivariate data are used to gain a qualitative understanding of the multiple factors that interact in real life situations, including, but not limited to, population characteristics, environmental considerations, production variables etc.
- understand how technology has enabled the collection, visualisation and analysis of large data sets to inform decision-making processes in public, commercial and academic sectors
- develop skills in interpretation and critical evaluation of methodology including justifying the techniques used for statistical problem solving
- apply appropriate mathematical and statistical formulae, as set out in appendix 1 and appendix 2

Detailed content statements

Overview

4. AS and A level statistics specifications assume a basic level of numerical skills as listed in appendix 3, as studied in the GCSE (9-1) mathematics subject content. The knowledge and skills required for AS statistics are shown in paragraph 8 with the knowledge and skills required for A level statistics in both paragraphs 8 and 9.

5. Specifications must make explicit reference to how the assessment will focus on the underpinning principles of the statistical enquiry cycle, as detailed in appendix 4, developed through investigations completed as part of the programme of study. Specifications should give students the opportunity to understand that different approaches, including the use of technology, may be appropriate at each stage of the statistical enquiry cycle, and that statistical conclusions are developed through an iterative process of retesting and refinement. Specifications should give students the opportunity to develop an understanding of how the subject content is applied in decision making processes used in the world around them by using realistic data taken from authentic contexts in their studies.

6. Students must develop the skills required to interpret data presented in summary or graphical form and use data to investigate questions arising in authentic contexts. This includes an understanding of the importance of primary and secondary data sourcing techniques.

Use of technology

7. Calculators used must include the ability to compute summary statistics and access probabilities from standard statistical distributions.

AS statistics

8. Content required for AS statistics is shown below. This, assessed in the context of the statistical enquiry cycle, represents 100% of the AS content. AS and A level specifications must require students to:

A1.1 - numerical measures, graphs and diagrams

- interpret statistical diagrams including bar charts, stem and leaf diagrams, box and whisker plots, cumulative frequency diagrams, histograms (with either equal or unequal class intervals), time series and scatter diagrams
- know the features needed to ensure an appropriate representation of data using the above diagrams, and how misrepresentation may occur
- justify appropriate graphical representation and comment on those published

- compare different data sets, using appropriate diagrams or calculated measures of central tendency and spread: mean, median, mode, range, interquartile range, percentiles, variance and standard deviation
- calculate measures using calculators and manual calculation as appropriate
- identify outliers by inspection and using appropriate calculations
- determine the nature of outliers in reference to the population and original data collection process
- appreciate that data can be misrepresented when used out of context or through misleading visualisation

A1.2 - probability

- know and use language and symbols associated with set theory in the context of probability
- represent and interpret probabilities using tree diagrams, Venn diagrams and two-way tables
- calculate and compare probabilities: single, independent, mutually exclusive and conditional probabilities
- use and apply the laws of probability to include conditional probability
- determine if two events are statistically independent

A1.3 - population and samples

- know both simple (without replacement) and unrestricted (with replacement) random samples
- know how to obtain a random sample using random numbers tables or random numbers generated on a calculator
- evaluate the practical application of random and non-random sampling techniques: simple random, systematic, cluster, judgemental and snowball, including the use of stratification (in proportional and disproportional ratios) prior to sampling taking place
- know the advantages and limitations of sampling methods
- make reasoned choices with reference to the context in which the sampling is to take place, examples include, but are not limited to: market research, exit polls, experiments and quality assurance
- understand the practical constraints of collecting unbiased data

A1.4 - introduction to probability distributions

- know and use terms for variability: random, discrete, continuous, dependent and independent
- calculate probabilities and determine expected values, variances and standard deviations for discrete distributions
- use discrete random variables to model real-world situations
- know the properties of a continuous distribution

- interpret graphical representations or tabulated probabilities of characteristic discrete random variables
- interpret rectilinear graphical representations of continuous distributions

A1.5 - binomial distribution

- know when a binomial model is appropriate (in real world situations including modelling assumptions)
- know methods to evaluate or read probabilities using formula and tables
- calculate and interpret the mean and variance

A1.6 - normal distribution

- know the specific properties of the normal distribution, and know that data from such an underlying population would approximate to having these properties, with different samples showing variation
- apply knowledge that approximately $\frac{2}{3}$ of observations lie within $\mu \pm \sigma$, and equivalent results for 2σ and 3σ
- determine probabilities and unknown parameters with a normal distribution
- apply the normal distribution to model real world situations
- use the fact that the distribution of \bar{X} has a normal distribution if X has a normal distribution
- use the fact that the normal distribution can be used to approximate a binomial distribution under particular circumstances

A1.7 - correlation and linear regression

- calculate (only using appropriate technology - calculator) and interpret association using Spearman's rank correlation coefficient or Pearson's product moment correlation coefficient
- use tables to test for significance of a correlation coefficient
- know the appropriate conditions for the use of each of these methods of calculating correlation and determine an appropriate approach to assessing correlation in context
- calculate (only using appropriate technology - calculator) and interpret the coefficients for a least squares regression line in context; interpolation and extrapolation, and use of residuals to evaluate the model and identify outliers

A1.8 - introduction to hypothesis testing

- use and demonstrate understanding of the terms parameter, statistic, unbiased and standard error
- know and use the language of statistical hypothesis testing: null hypothesis, alternative hypothesis, significance level, test statistic, 1-tail test, 2-tail test, critical value, critical region, and acceptance region and p-value

- know that a sample is being used to make an inference about the population and appreciate the need for a random sample and of the necessary conditions
- choose the appropriate hypothesis test to carry out in particular circumstances
- conduct a statistical hypothesis test for the proportion in the binomial distribution and interpret the results in context using exact probabilities or, where appropriate, a normal approximation
- conduct a statistical hypothesis test for the mean of a normal distribution with known or assumed, from a large sample, variance and interpret the results in context
- know the importance of appropriate sampling when using hypothesis tests and be able to critique the conclusions drawn from rejecting or failing to reject a null hypothesis by considering the test performed

A1.9 - contingency tables

- construct contingency tables from real data, combining data where appropriate, and interpret results in context
- use a χ^2 test with the appropriate number of degrees of freedom to test for independence in a contingency table and interpret the results of such a test
- know that expected frequencies must be greater than, or equal to, 5 for a χ^2 test to be carried out and understand the requirement for combining classes if that is not the case

A1.10 - one and two sample non-parametric tests

- use sign or Wilcoxon signed-rank tests to investigate population median in single sample tests and also to investigate for differences using a paired model
- use the Wilcoxon rank-sum test to investigate for difference between independent samples

A level statistics

9. Content required for A level statistics is shown in the AS statistics paragraphs A1.1 to A1.10, plus paragraphs A2.1 to A2.11. The content set out in these paragraphs, assessed in the context of the statistical enquiry cycle, represent 100% of the A level content. A level specifications must require students to:

A2.1 - Bayes' theorem

- calculate and use conditional probabilities to include Bayes' theorem for up to three events, including the use of tree diagrams

A2.2 - probability distributions

- know the use and validity of distributions which could be appropriate in a particular real-world situation: binomial, normal, Poisson and exponential

- evaluate the mean and variance of linear combinations of independent random variables through knowledge that if X_i are independently distributed (μ_i, σ_i^2) then $\sum a_i X_i$ is distributed $(\sum a_i \mu_i, \sum a_i^2 \sigma_i^2)$
- evaluate probabilities for linear combinations of two or more independent normal distributions and apply this knowledge to practical situations

A2.3 - experimental design

- know and discuss issues involved in experimental design: experimental error, randomisation, replication, control and experimental groups, and blind and double blind trials
- know the benefits of use of paired comparisons and blocking to reduce experimental error
- use completely random and randomised block designs

A2.4 - sampling, estimates and resampling

- use and demonstrate understanding of terms parameter, statistic, unbiased and standard error
- know the use of the central limit theorem in the distribution of \bar{X} where the initial distribution, X , is not normally distributed and the sample is large

A2.5 - hypothesis testing, significance testing, confidence intervals and power

- use confidence intervals for the mean using z or t as appropriate, interpreting results in practical contexts
- know that a change in sample size will affect the width of a confidence interval
- evaluate the strength of conclusions and misreporting of findings from hypothesis tests, including the calculation and importance of the power of a hypothesis test
- know that sample size can be changed to potentially elicit appropriate evidence in a hypothesis test
- interpret type I and type II errors, in hypothesis testing and know their practical meaning
- calculate the risk of a type II error
- know the difference and advantages of using critical regions or p-values as appropriate in real-life contexts in all tests in these subject content

A2.6 - hypothesis testing for 1 and 2 samples

- know how to apply knowledge about carrying out hypothesis testing to conduct tests for the:
 - mean of a normal distribution with unknown variance using the t distribution
 - difference of two means for two independent normal distributions with known variances

- difference of two means for two independent normal distributions with unknown but equal variances
- difference between two binomial proportions
- interpret results for these tests in context

A2.7 - paired tests

- use sign, Wilcoxon signed-rank or paired t -test, understanding appropriate test selection and interpreting the results in context

A2.8 - exponential and Poisson distributions

- determine when a Poisson model is appropriate (in real world situations including modelling assumptions)
- determine when an exponential distribution is appropriate (and its relationship to the Poisson distribution as a model of the times between randomly occurring Poisson events)
- evaluate probabilities for Poisson and exponential distributions and know the corresponding mean and variance

A2.9 - goodness of fit

- conduct a statistical goodness of fit test for binomial, Poisson, normal and

Exponential distributions or for a specified discrete distribution using $\sum \frac{(O - E)^2}{E}$ as an approximate χ^2 statistic

A2.10 - analysis of variance

- conduct one-way analysis of variance, using a completely randomised design with appreciation of the underlying model with additive effects and experimental errors distributed as $N(0, \sigma^2)$
- conduct two-way analysis of variance without replicates, using a randomised block design with blocking
- identify assumptions and interpretations in context

A2.11 - effect size

- know the notion of effect size as a complementary methodology to standard significance testing, and apply in authentic contexts
- know and use Cohen's d in simple situations

Appendix 1

Statistical formulae for AS and A level statistics that students are expected to learn and must not be given in the assessment. AS students will be expected to learn the statistical formulae that relates to AS content, and will not be expected to learn the statistical formulae that relates only to A level content.

Content Reference	Formula required
A1.1	Calculating the angle for a sector in a pie chart: $\frac{x}{total} \times 360$
A1.1	Frequency density for a histogram: $frequency\ density = \frac{frequency}{class\ width}$
A1.1	Calculation of arithmetic mean: $\bar{x} = \frac{\sum fx}{\sum f}$
A1.1	Range = highest value – lowest value
A1.1	Interquartile range (IQR) = upper quartile – lower quartile
A1.1	Identification of an outlier: Lower outlier is < LQ – 1.5IQR Upper outlier is > UQ + 1.5IQR Outlier is also outside $\mu \pm 3\sigma$
A1.2	Formulae for independent events: $P(A \cap B) = P(A)P(B)$ $P(A B) = P(A)$ and $P(B A) = P(B)$
A1.3	In order to carry out stratification, calculating the percentage or proportion of an amount: $\frac{x}{100} \times amount$
A1.4	Properties of discrete random variables: expectation (mean): $E(X) = \mu = \sum x_i p_i$ variance: $Var(X) = \sigma^2 = \sum (x_i - \mu)^2 p_i = \sum x_i^2 p_i - \mu^2 = E(X^2) - \mu^2$
A2.6	Other confidence intervals: several variations on estimate $\pm t$ or z value \times standard error according to the particular confidence interval

Appendix 2

Statistical formulae for AS and A level statistics that students are expected to be familiar with and will be given in the assessment, either with the question or as a separate formulae sheet or booklet. AS students will be expected to be familiar with the statistical formulae that relates to AS content, and will not be expected to be familiar with the statistical formulae that relates only to A level content.

Content Reference	Formula required
A1.1	Population variance = $\frac{1}{N} \sum (x - \mu)^2$ Population standard deviation = $\sqrt{\frac{1}{N} \sum (x - \mu)^2}$
A1.1	Sample variance = $\frac{1}{n-1} \sum (x - \bar{x})^2$ Sample standard deviation = $\sqrt{\frac{1}{n-1} \sum (x - \bar{x})^2}$
A1.5	Binomial probability calculations: $P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$ Mean = np Variance = $np(1-p)$
A1.7	Test statistic for a mean using normal distribution: $\frac{\bar{X} - \mu}{\frac{\sigma}{\sqrt{n}}} \sim N(0,1)$ Test statistic for a binomial proportion using normal distribution: $\frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} \sim N(0,1)$
A1.8	Formula for chi-squared test $\sum \frac{(O_i - E_i)^2}{E_i}$
A2.1	Bayes' theorem for up to three events: $P(A_j B) = \frac{P(A_j) \times P(B A_j)}{\sum_{i=1}^n P(A_i) \times P(B A_i)}$
A2.2	The Poisson probability formula $P(X = x) = e^{-\lambda} \frac{\lambda^x}{x!}$ and knowledge of the mean and variance both being λ

Content Reference	Formula required
A2.2	The exponential cumulative probability formula: $P(X \leq x) = 1 - e^{-\lambda x}$ and knowledge of the mean and variance being $\frac{1}{\lambda}$ and $\frac{1}{\lambda^2}$ respectively
A2.3	$E(XY) = E(X)E(Y)$ $\text{Var}(aX \pm bY) = a^2 \text{Var}(X) + b^2 \text{Var}(Y)$ but $E(X+Y) = E(X) + E(Y)$ not given
A2.7	Test statistic for a mean using t distribution: $\frac{\bar{X} - \mu}{\frac{S}{\sqrt{n}}} \sim t_{n-1}$
A2.7	Test statistic for difference of two independent normal means with known variances: $\frac{(\bar{X} - \bar{Y}) - (\mu_x - \mu_y)}{\sqrt{\frac{\sigma_x^2}{n_x} + \frac{\sigma_y^2}{n_y}}} \sim N(0, 1)$
A2.7	Test statistic for difference of two independent normal means with unknown but equal variance: $\frac{(\bar{X} - \bar{Y}) - (\mu_x - \mu_y)}{\sqrt{S_p^2 \left(\frac{1}{n_x} + \frac{1}{n_y} \right)}} \sim t_{n_x + n_y - 2}$ where $S_p^2 = \frac{(n_x - 1)S_x^2 + (n_y - 1)S_y^2}{n_x + n_y - 2}$
A2.7	Test statistic for the difference in two binomial proportions: $\frac{p_1 - p_2}{s.error}$ where s. error = $\sqrt{p \times (1 - p) \times \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}$ where $p = \frac{p_1 \times n_1 + p_2 \times n_2}{n_1 + n_2}$
A2.8	Paired <i>t</i> -test:

Content Reference	Formula required
	$\frac{\bar{X} - \mu}{\frac{S}{\sqrt{n}}} \sim t_{n-1}$
A2.9	<p>Test for association and goodness of fit test:</p> $\sum \frac{(O_i - E_i)^2}{E_i}$ <p>is approximately distributed as X^2</p>
A2.10	<p>Analysis of variance (one-way and two-way):</p> <p>one-factor model $x_{ij} = \mu + \alpha_i + \varepsilon_{ij}$, where $\varepsilon_{ij} \sim N(0, \sigma^2)$</p> <p>total sum of squares $SS_T = \sum_i \sum_j x_{ij}^2 - \frac{T^2}{n}$</p> <p>between groups sum of squares $SS_B = \sum_i \frac{T_i^2}{n_i} - \frac{T^2}{n}$</p> <p>two-factor model (with m rows and n columns)</p> <p>$x_{ij} = \mu + \alpha_i + \beta_j + \varepsilon_{ij}$, where $\varepsilon_{ij} \sim N(0, \sigma^2)$</p> <p>total sum of squares $SS_T = \sum_i \sum_j x_{ij}^2 - \frac{T^2}{mn}$</p> <p>between rows sum of squares $SS_R = \sum_i \frac{R_i^2}{n} - \frac{T^2}{mn}$</p> <p>between columns sum of squares $SS_C = \sum_j \frac{C_j^2}{m} - \frac{T^2}{mn}$</p>
A2.11	<p>Cohen's d formula:</p> $d = \frac{(\bar{x}_1 - \bar{x}_2)}{s}$ <p>where $s = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}}$</p>
A2.12	<p>Spearman's correlation coefficient:</p> $r_s = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$
A2.12	<p>Product moment correlation coefficient:</p>

Content Reference	Formula required
	$r = \frac{S_{xy}}{\sqrt{S_{xx} \times S_{yy}}} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\{\sum (x_i - \bar{x})^2\} \{\sum (y_i - \bar{y})^2\}}} = \frac{\sum x_i y_i - \frac{(\sum x_i)(\sum y_i)}{n}}{\sqrt{\left(\sum x_i^2 - \frac{(\sum x_i)^2}{n}\right) \left(\sum y_i^2 - \frac{(\sum y_i)^2}{n}\right)}}$
A2.12	<p>Coefficients for least squares regression line: least squares regression line of y on x is $y = a + bx$, where $a = \bar{y} - b\bar{x}$</p> <p>the regression coefficient of y on x is $b = \frac{S_{xy}}{S_{xx}} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}$</p>

Appendix 3

The numerical skills, developed in GCSE (9-1) mathematics, required for AS and A level statistics:

Integers, fractions, decimals and percentages

- work interchangeably with terminating decimals and their corresponding fractions (such as 3.5 and $\frac{7}{2}$ or 0.375 or $\frac{3}{8}$), and recognise that some fractions can be written as recurring decimals
- identify and work with fractions in ratio problems
- interpret fractions and percentages as operators

Structure and calculation

- order positive integers, decimals and fractions
- understand and use the symbols =, \neq , <, >, \leq and \geq
- apply the four operations to integers, decimals and simple fractions (proper and improper), and mixed numbers
- understand and use place value (e.g. when working with very large or very small numbers, and when calculating with decimals)
- recognise, use and manipulate numbers in standard form
- recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions; use conventional notation for priority of operations, including brackets, powers, roots and reciprocals)
- substitute numerical values into formulae and expressions, including scientific formulae
- understand and use standard mathematical formulae, and rearrange formulae to change the subject
- solve algebraic equations, including simultaneous equations
- work with coordinates on Cartesian grid

Measures and accuracy

- use standard units of mass, length, time, money and other measures (including standard compound measures) using decimal quantities where appropriate
- estimate answers and check calculations using approximation and estimation, including answers obtained using technology
- use compound units such as speed, rates of pay and unit pricing including working out a unit for a rate

- round numbers and measures to an appropriate degree of accuracy (e.g. to a specified number of decimal places or significant figures), and use inequality notation to specify simple error intervals due to truncation or rounding

Ratio, proportion and rates of change

- express one quantity as a fraction of another, where the fraction is less than 1 or greater than 1
- use ratio notation, including reduction to simplest form
- divide a given quantity into two parts in a given part, part or part, and whole ratio; express the division of a quantity into two parts as a ratio; and apply ratio to real contexts and problems (such as those involving probability)
- relate ratios to fractions and vice versa
- define percentage as 'number of parts per hundred'; interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively; express one quantity as a percentage of another; and compare two quantities using percentages

Appendix 4

Specifications must encourage the application of techniques within the framework of the statistical enquiry cycle using real data taken from authentic contexts.

Specifications must require students to understand the importance of initial planning when designing a line of enquiry or investigation including:

- identifying factors that may be related to the problem under investigation
- defining a question or hypothesis (or hypotheses) to investigate
- deciding what data to collect, and how to collect and record it, giving reasons
- engaging in exploratory data analysis in order to investigate the situation
- developing a strategy for how to process and represent the data giving reasons
- justifying the proposed plan with regards ensuring a lack of bias

Specifications must enable students to recognise the constraints involved in sourcing data including:

- when designing unbiased collection methods for primary sample data
- when researching sources of secondary data, including from reference publications, the internet and the media
- recognise the importance of declaring the data collection methodology, including appreciating the importance of acknowledging sources
- appreciating the inherent bias that may be incorporated through the use of leading questions either by accident or through agenda driven design

Students must understand a range of techniques in order to process, represent and discuss data including:

- organising and processing data, including an understanding of how technology can be used
- make inferences about the population using appropriately chosen diagrams and summary measures to represent data including an understanding of outputs generated by appropriate technology
- appreciating how to avoid misrepresentation of data

Students must appreciate the need to consider the context of the problem when interpreting results:

- analysing/interpreting diagrams and calculations/measures
- drawing together conclusions that relate to the questions and hypotheses addressed
- using appropriate tests to determine the statistical significance of the findings
- discussing the reliability of findings

Specifications must require students to show an understanding of the importance of the clear and concise communication of findings and key ideas, and awareness of target audience.

Students must be able to understand the importance of evaluating statistical work including:

- identifying weaknesses in approaches used to collect or display data
- recognising the limitations of findings by considering sample size and sampling technique
- suggesting improvements to statistical processes or presentation
- refining processes to elicit further clarification of the initial hypothesis



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